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Fourth Semester B.E. Degree Examination, December 2012
Control Systems

Time: 3 hrs.

Max. Marks:100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART – A

- 1 a. Compare linear and non-linear control system. (04 Marks)
- b. For the two port network shown in Fig. Q1 (b), obtain the transfer functions, i) $\frac{V_2(s)}{V_1(s)}$ and ii) $\frac{V_1(s)}{I_1(s)}$ (08 Marks)

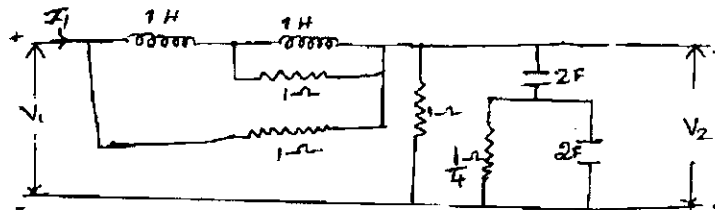


Fig. Q1 (b)

- c. For the rotational system shown in Fig. Q1 (c), i) Draw the mechanical network ii) Write the differential equations iii) Obtain torque to voltage analogy. (08 Marks)

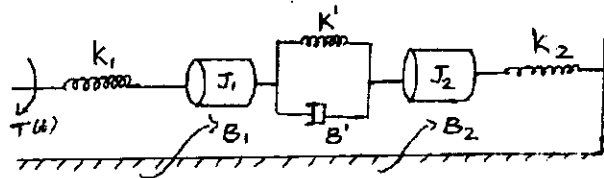


Fig. Q1 (c)

- 2 a. Illustrate how to perform the following, in connection with block diagram reduction rules:
- i) Shifting a take-off point after a summing point.
 - ii) Shifting a take-off point before a summing point. (04 Marks)
- b. The performance equations of a controlled system are given by the following set of linear algebraic equations:
- i) Draw the block diagram.
 - ii) Find the overall transfer function $\frac{C(s)}{R(s)}$ using block diagram reduction technique.

$$E_1(s) = R(s) - H_3(s)C(s); E_2(s) = E_1(s) - H_1(s)E_4(s); E_3(s) = G_1(s)E_2(s) - H_2(s)C(s)$$

$$E_4(s) = G_2(s)E_3(s); C(s) = G_3(s)E_4(s) \quad (08 \text{ Marks})$$

- c. Draw the corresponding signal flow graph for the given block diagram is shown in Fig. Q2 (c) and obtain the overall transfer function by Mason's gain formula. (08 Marks)

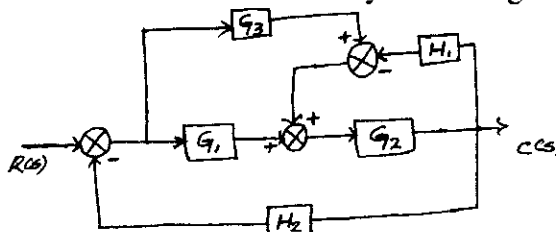


Fig. Q2 (c)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. 2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.

- 3 a. Derive the expression for peak time. (04 Marks)
 b. The loop transfer function of a feed back control system is given by,

$$G(s)H(s) = \frac{100}{s^2(s+4)(s+12)}$$

- i) Determine the static error co-efficients.
 ii) Determine the steady state error for the input $r(t) = 2t^2 + 5t + 10$ (08 Marks)
 c. A system is given by differential equation, $\frac{d^2y(t)}{dt^2} + 4\frac{dy(t)}{dt} + 8y(t) = 8x(t)$.

Where $y(t)$ = output and $x(t)$ = input.

- Determine i) peak time ii) peak over shoot iii) settling time
 iv) expression of the output response. (08 Marks)

- 4 a. Define the term stability applied to control system and what is the difference between absolute stability and relative stability. (04 Marks)

- b. Using Routh's criterion determine the stability of following systems:
 i) Its open loop transfer function has poles at $s = 0, s = -1, s = -3$ and zero at $s = -5$. Gain $K = 10$.

- ii) It is a type one system with an error constant of 10 sec^{-1} and poles at $s = -3$ and $s = -6$ (08 Marks)

- c. Using RH criterion determine the stability of the system having the characteristic equation, $s^4 + 10s^3 + 36s^2 + 70s + 75 = 0$ has roots more negative than $s = -2$. (08 Marks)

PART - B

- 5 a. The open-loop transfer function of a feed back control system in $G(s)H(s) = \frac{K}{(s+1)(s+2)(s+3)}$, check whether the following points are on the root locus. If

so, find the value of K at these points. i) $s = -1.5$ ii) $s = -0.5 + j2$ (06 Marks)

- b. Sketch the root locus plot for a negative feed back control system characterized by an open loop transfer function, $G(s)H(s) = \frac{K}{s(s+3)(s^2+3s+11.2s)}$. Comment on stability. (14 Marks)

- 6 a. State the advantages and limitations of frequency domain approach. (06 Marks)

- b. Determine the transfer function, of a system whose asymptotic gain plot is shown in Fig. Q6 (b). (10 Marks)

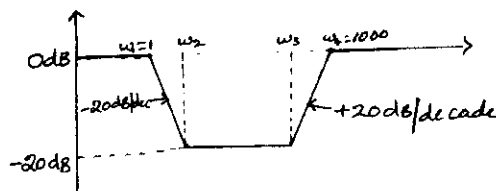


Fig. Q6 (b)

- c. List the effects of lead compensation. (04 Marks)

- 7 a. Draw polar plot of $G(s)H(s) = \frac{100}{(s+2)(s+4)(s+8)}$. (04 Marks)

- b. Explain Nyquist stability criterion. (06 Marks)

- c. Sketch the Nyquist plot for, $GH(s) = \frac{K}{s(s+1)(s+2)}$. Then, find the range of K for closed loop stability. (10 Marks)

- 8 a. Define the following terms: i) state ii) state variables iii) state space. (06 Marks)

- b. List the advantages of state variable analysis. (04 Marks)

- c. Obtain the state transition matrix for, $A = \begin{bmatrix} 0 & -1 \\ 2 & -3 \end{bmatrix}$. (10 Marks)
